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# FINA 1082 Financial Management

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## Session 3

### Valuation of Equity Securities

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## At different levels business decisions involves valuation

**Capital Budgeting:** involves consideration of how a particular project will affect firm value.

**Strategic planning:** focuses on how value is influenced by larger sets of actions.

**Security analysts:** conduct valuation to support their buy/sell decisions, and potential acquirers.

## Basics in Valuation Approaches

- perception that markets are **inefficient** and make mistakes in assessing value
- an assumption about **how and when** these inefficiencies will get corrected

In an efficient market, the **market price is the best estimate** of value.

The purpose of any valuation model is then the **justification** of this value.

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*Valuation objective is to search for “true” value*

Valuations are biased. The question is how much and in which direction.

The direction and magnitude of the bias is *directly proportional* to who pays you and how much you are paid.

# Valuation Approaches

**Discounted Cash Flow:** value of any asset is estimated by computing the PV of the expected cash flows on that asset, discounted back at a rate that reflects the riskiness of the cash flows (measure of the intrinsic value of an asset).

**Relative Valuation:** The value of any asset can be estimated by looking how similar assets are priced in the market place.

# Academic Studies

Mainly focus on the comparison of **two model approaches**:

- Discounted Dividends
- Discounted Cash Flows

Ratios or multiple based models are discussed in isolation or in addition of the three previous models.

## Main valuation models:

**Discounted Dividends:** This approach expresses the value of firm's equity as the present value of forecasted future dividends.

**Discounted Cash Flow (DCF):** involves detailed production of multiple year forecasts of cash flows. Cash Flows are then discounted at the firm's estimated cost of capital to arrive at an estimated present value.

**\*Discounted Abnormal Earnings:** Value of firm's equity is expressed as the sum of its book value and the present value of the forecasted abnormal earnings.

**\*Discounted abnormal earnings growth:** Value of the firm's equity as the sum of its capitalized next-period earnings forecast and the present value of forecasted abnormal earnings growth beyond the next period.

**\*Real Options:** Contingent Claim (Option) Valuation

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**Valuation based on price multiples:** Current measure of performance or single forecast of performance is converted into a value by applying an appropriate **price multiple derived from the value of comparable firms.**

**Example:** firm value can be estimated by applying a **price-to-earnings ratio** to a forecast of the firm's earnings for the coming year. Other commonly used multiples include **price-to-book ratios and price-to-sales ratios.**

# Discounted Cashflow Valuation

$$\text{Value} = \sum_{t=1}^n \frac{CF_t}{(1+r)^t}$$

Where

- $CF_t$  is the cash flow in period  $t$ ,
- $r$  is the discount rate appropriate given the riskiness of the cash flow, and
- $t$  is the life of the asset.

For an asset to have value, the expected cash flows have to be **positive** some time over the **life of the asset**.

Assets that generate cash flows early in their life will **be worth more than assets that generate cash flows later**; the later may however have greater growth and higher cash flows to compensate.

# Characteristics of Ordinary Shares

Ordinary shares typically provide investors with an infinite stream of uncertain cash flows or dividends -  $D_1, D_2, \dots, D_n, \dots$ . The price of ordinary shares today is the present value of all future expected dividends discounted at the “appropriate” required rate of return (or discount rate)

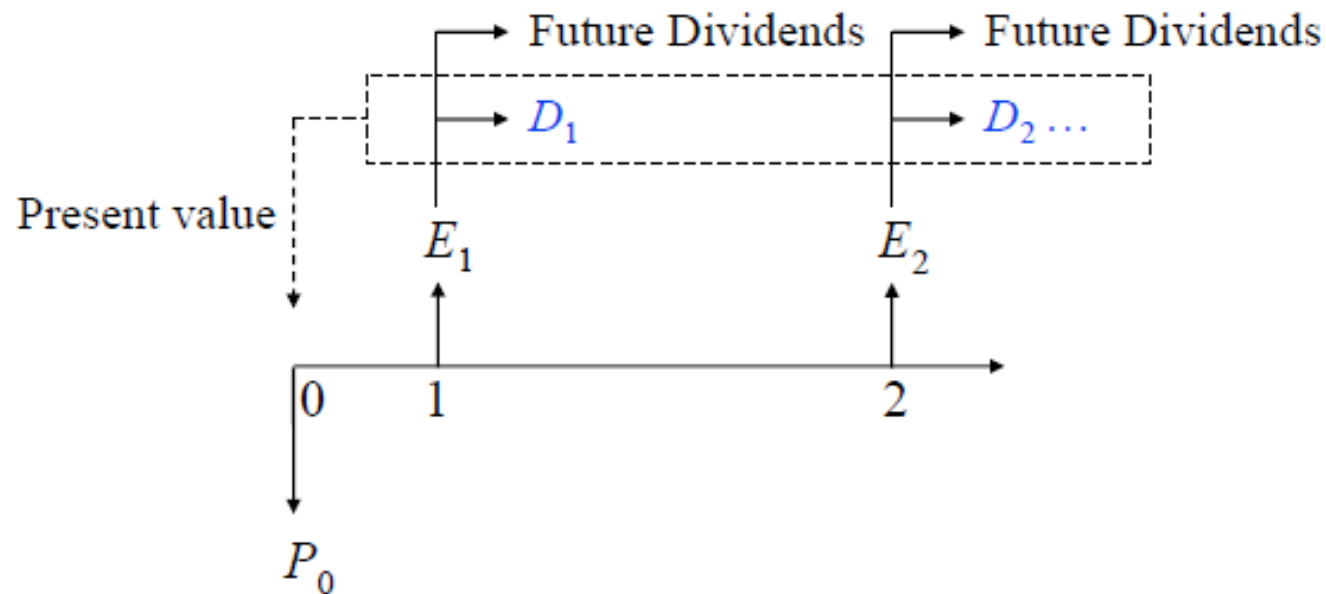
$$P_0 = \sum_{t=1}^N \frac{CF_t}{(1 + k_e)^t}$$

where  $k_e$  is the rate of return required by investors for the time value and risk associated with the security's cash flows (CFT)

What cash flows are relevant?

# Characteristics of Ordinary Shares

Need to consider dividends, which are paid from earnings



## Pricing Ordinary Shares

In a one period framework, the stock price is equal to the sum of the next period's dividend and the expected price discounted at the required return

$$P_0 = \frac{D_1 + P_1}{1 + k_e} \quad \text{and} \quad P_1 = \frac{D_2 + P_2}{1 + k_e} \quad \text{and} \quad P_t = \frac{D_{t+1} + P_{t+1}}{1 + k_e}$$

Over any period, the expected rate of return ( $k_e$ ) is

$$k_e = \frac{D_{t+1} + P_{t+1}}{P_t} - 1 = \frac{D_{t+1}}{P_t} + \frac{P_{t+1} - P_t}{P_t}$$

$k_e = \text{Dividend yield} + \text{Percent price change}$

## Pricing Ordinary Shares

**Example:** The price and dividend per share for OzCo Ltd next period are expected to be \$5.00 and \$0.50, respectively. If the expected return on these shares is 10% p.a. what is OzCo's current stock price? If the current price changes to \$4.80 what has happened to the expected return on these shares? Why?

Given:  $P_{t+1} = \$5.00$ ,  $D_{t+1} = \$0.50$  and  $k_e = 10\%$

$$P_t = \frac{0.50 + 5.00}{1 + 0.10} = \$5.00$$

If the current price changes to \$4.80, the expected return rises to

$$k_e = \frac{0.50 + 5.00}{4.80} - 1 = 14.6\%$$

**Note that prices and expected returns are inversely related**

## Pricing Ordinary Shares

The stock price over periods 0, 1 and 2 can be written as

$$P_0 = \frac{D_1 + P_1}{1 + k_e} \quad \text{and} \quad P_1 = \frac{D_2 + P_2}{1 + k_e} \quad \text{and} \quad P_2 = \frac{D_3 + P_3}{1 + k_e}$$

Substituting  $P_2$  and  $P_1$  recursively, we get  $P_0$  as

$$P_0 = \frac{D_1}{1 + k_e} + \frac{D_2}{(1 + k_e)^2} + \frac{D_3 + P_3}{(1 + k_e)^3}$$

- The **current dividend** ( $D_0$ ) is not relevant to our estimate of the **current price** - all prices estimated are ex-dividend prices
- Ex-dividend prices are prices after the current period's dividend has been paid

# Pricing Ordinary Shares

Extending the above process to H periods, we get

$$P_0 = \frac{D_1}{1 + k_e} + \frac{D_2}{(1 + k_e)^2} + \frac{D_3}{(1 + k_e)^3} + \dots + \frac{D_H + P_H}{(1 + k_e)^H}$$

$$P_0 = \sum_{t=1}^H \frac{D_t}{(1 + k_e)^t} + \frac{P_H}{(1 + k_e)^H}$$

$$\text{As } H \rightarrow \infty, PV(P_H) \rightarrow 0$$

$$P_0 = \sum_{t=1}^{\infty} \frac{D_t}{(1 + k_e)^t}$$

Market analysts often make simplifying assumptions about future expected dividends

# Constant Dividend Growth Model

A constant growth rate in dividends implies

$$D_2 = D_1(1 + g), D_3 = D_1(1 + g)^2, \dots, D_t = D_1(1 + g)^{t-1}$$

Substituting the above dividends in the expression for  $P_0$  we get

$$P_0 = \sum_{t=1}^{\infty} \frac{D_t}{(1 + k_e)^t} = \sum_{t=1}^{\infty} \frac{D_1(1 + g)^{t-1}}{(1 + k_e)^t}$$

$$\text{As } t \rightarrow \infty, \sum_{t=1}^{\infty} \frac{(1 + g)^{t-1}}{(1 + k_e)^t} \rightarrow \frac{1}{k_e - g}$$

The above expression simplifies to

$$P_0 = \frac{D_1}{k_e - g} \quad \text{where } k_e > g \quad \text{or} \quad P_t = \frac{D_{t+1}}{k_e - g}$$

# Constant Dividend Growth Model

**Application 1:** Assume that year 0 is the end of 2004. Telstra Ltd is expected to pay annual dividends of \$0.26 in 2005 (year 1). Assume that this dividend grows at an annual rate of 5% in the foreseeable future and investors require a return of 10% p.a.

- a) Estimate Telstra's stock price today
- b) What is Telstra's price expected to be at the end of 2005?
- c) Based on Telstra's current price of \$4.75, what is the constant dividend growth rate implied?
- d) How sensitive is the price estimate to different assumptions regarding the growth in dividends over time?
- e) How sensitive is the price estimate to different assumptions regarding the required rate of return?

# Constant Dividend Growth Model

Given:  $D_1 = 0.26$ ,  $g = 0.05$  and  $k_e = 0.10$

a)  $P_0 = 0.26 / (0.10 - 0.05) = \$5.20$

b)  $P_1 = D_2 / (k_e - g) = 0.26(1.05) / (0.10 - 0.05) = \$5.46$  (a 5% rise)

c)  $k_e = D_1 / P_0 + g$  or  $g = k_e - D_1 / P_0$   
 $g = 0.10 - 0.26 / 4.75 = 0.0453$  or 4.5%

d) Sensitivity of Telstra's price to changes in expectations of  $g$

$g = 3\%: P_0 = 0.26 / (0.10 - 0.03) = \$3.71$  (-28.7%)

$g = 4\%: P_0 = 0.26 / (0.10 - 0.04) = \$4.33$  (-16.7%)

$g = 5\%: P_0 = 0.26 / (0.10 - 0.05) = \$5.20$

$g = 6\%: P_0 = 0.26 / (0.10 - 0.06) = \$6.50$  (+25.0%)

$g = 7\%: P_0 = 0.26 / (0.10 - 0.07) = \$8.67$  (+66.7%)

# Constant Dividend Growth Model

Sensitivity of Telstra's price to changes in  $k_e$

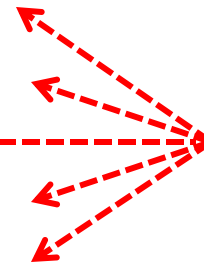
$$k_e = 8\%: P_0 = 0.26 / (0.08 - 0.05) = \$8.67 (+66.7\%)$$

$$k_e = 9\%: P_0 = 0.26 / (0.09 - 0.05) = \$6.50 (+25.0\%)$$

$$k_e = 10\%: P_0 = 0.26 / (0.10 - 0.05) = \$5.20$$

$$k_e = 11\%: P_0 = 0.26 / (0.11 - 0.05) = \$4.33 (-16.7\%)$$

$$k_e = 12\%: P_0 = 0.26 / (0.12 - 0.05) = \$3.71 (-28.7\%)$$



- Price estimates are very sensitive to assumptions regarding future dividends, growth in dividends and required rate of return
- It is often more realistic to assume a variable growth rate in dividends with higher initial growth in dividends followed by subsequent lower (or zero) growth in dividends

## Variable Dividend Growth Model

**Application 2:** In the previous application, assume that Telstra's current dividend of \$0.25 grows at 10% for 3 years and then stabilizes at 5% thereafter. What price should Telstra shares sell for today if the required rate of return remains at 10%?

**Three step procedure to estimate  $P_0$**

**Step 1:** Compute the dividends up to the point where  $g$  becomes constant (over years 1 to 4 in this case)

**Step 2:** Compute the price at the end of the year after which dividends grow at a constant rate (year 3 in this case)

**Step 3:** Add the present value of dividends from Step 1 to the present value of the price from Step 2 to get  $P_0$

# Variable Dividend Growth Model

Given:  $D_0 = \$0.25$ ,  $g_1 = 10\%$  over years 1 - 3,  
 $g_2 = 5\%$  from year 4 onwards,  $k_e = 10\%$

Step 1: Obtain dividends up to where  $g$  becomes constant

$$D_1 = 0.2500(1.10) = \$0.2750$$

$$D_2 = 0.2750(1.10) = \$0.3025$$

$$D_3 = 0.3025(1.10) = \$0.3328$$

$$D_4 = 0.3328(1.05) = \$0.3494$$

Step 2: Obtain  $P_n$  (after which dividend growth is constant)

$$P_3 = D_4 / (k_e - g_2) = 0.3494 / (0.10 - 0.05) = \$6.988$$

Step 3: Add the present values of dividends and  $P_n$  to get  $P_0$

$$P_0 = D_1 / (1 + k_e) + D_2 / (1 + k_e)^2 + (D_3 + P_3) / (1 + k_e)^3$$

$$P_0 = 0.2750 / 1.1 + 0.3025 / 1.1^2 + (0.3328 + 6.988) / 1.1^3 = \$6.00$$

## Equity versus Firm Valuation

- Value just the **equity stake** in the business.
- Value the entire business, which includes, besides equity, the **other claimholders in the firm**

# Equity Valuation

The value of equity is obtained by:

Discounting expected *cashflows to equity* (the residual cashflows after meeting all expenses, tax obligations and interest and principal payments) *at the cost of equity* (required return to shareholders).

$$\text{Value of Equity} = \sum_{t=1}^n \frac{\text{CF to Equity}_t}{(1+k_e)^t}$$

CF to Equity<sub>t</sub> = Expected Cashflow to Equity in period t

k<sub>e</sub> = Cost of Equity

**Note:** The dividend discount model is a specialized case of equity valuation

## Firm Valuation

The value of the firm is obtained by:

Discounting expected *cashflows to the firm* (the residual cashflows after meeting all operating expenses and taxes, but prior to debt payments) *at the WACC* (cost of the different components of financing used by the firm, weighted by their market value proportions)

$$\text{Value of Firm} = \sum_{t=1}^n \frac{\text{CF to Firm}_t}{(1+\text{wacc})^t}$$

### Adjusted Present Value approach:

Firm Value = Unlevered Firm Value + PV of tax benefits of debt - Expected Bankruptcy Cost

# Generic DCF Valuation Model

Firm is a stable growth  
Grows at constant rate  
forever

## Cash Flows

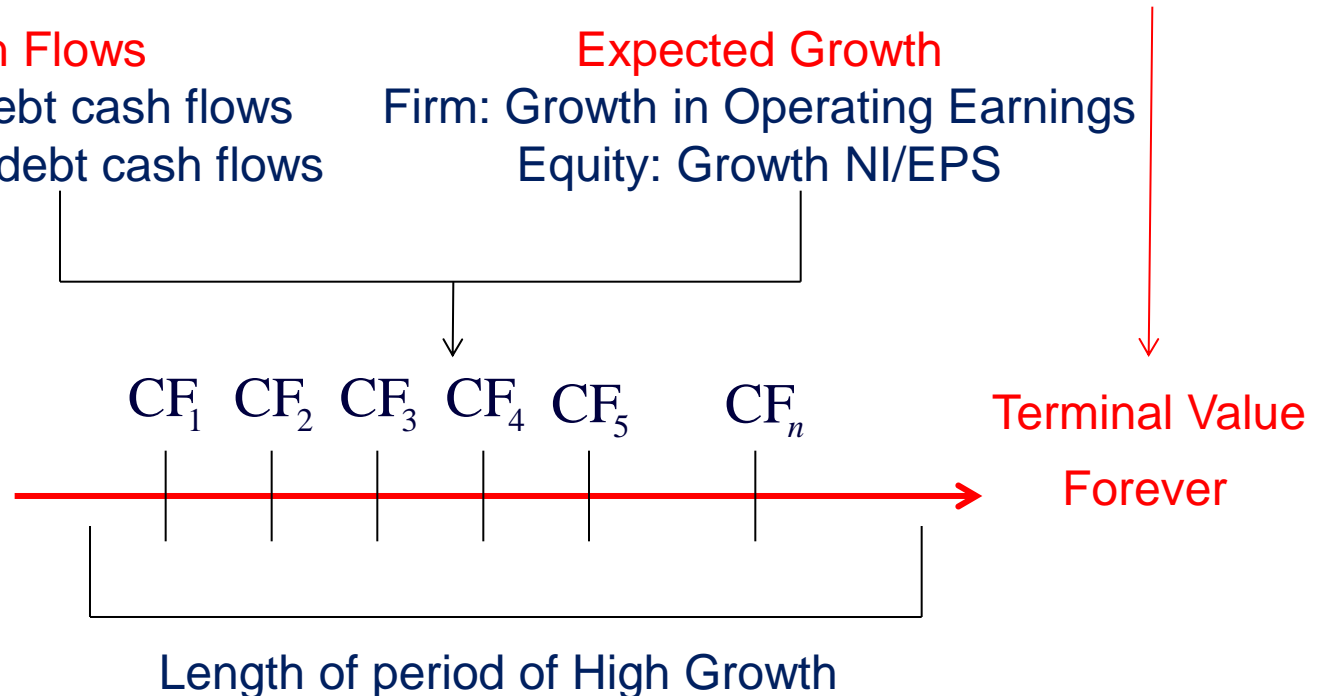
Firm: Pre-debt cash flows  
Equity: After-debt cash flows

## Expected Growth

Firm: Growth in Operating Earnings  
Equity: Growth NI/EPS

## Value

Firm: Value of Firm  
Equity: Value of Equity



## Discount Rate

Firm: Cost of Capital  
Equity: Cost of Equity

# Valuing ABC

Retention Ratio = 41.56%

ROE = 16%

$g = 4\%$  :  $ROE = 8.95\%$  (Cost of equity)

Beta = 1.00

Dividends

$EPS_0 = \$1.54$

Payout Ratio = 58.44%

$DPS_0 = \$0.90$

$$Payout = 1 - \frac{g}{ROE} = 1 - \frac{0.04}{0.0895} = 55.31\%$$

**Expected Growth**  
 $41.56\% \times 16.00\% = 6.65\%$

$$\begin{aligned} \text{Terminal value} &= \frac{EPS_6 \times Payout}{r - g} \\ &= \frac{\$2.12 \times 1.04 \times 0.553}{(0.895 - 0.04)} = \$24.69 \end{aligned}$$

$EPS_1 = \$1.64$   $EPS_2 = \$1.75$   $EPS_3 = \$1.87$   $EPS_4 = \$1.99$   $EPS_5 = \$2.12$

$DPS_1 = \$0.96$   $DPS_2 = \$1.02$   $DPS_3 = \$1.09$   $DPS_4 = \$1.16$   $DPS_5 = \$1.24$

Value of equity per  
share = **\$20.48**



Discount at Cost of Equity

$$4.95\% = 0.95 \times 4\% = 8.75\%$$

Risk free rate (Long term bond rate in USD ) + Beta  $\times$  Risk Premium

$$= 4.95\% + 0.95 \times 4\%$$

Risk Premium = Mature Market (4%) + Country Risk (0%)

## Discounted Free Cash Flow Model

Considers cash that is available to shareholders and lenders of the company.

Value of firm is determined as the present value of future cash flows plus excess cash and marketable securities, minus debt and preferred shares.

As valuation is completely dependent on future expectations, the model is vulnerable to mistakes in these assumptions. On average 82% of the firm value is determined by the terminal value.

$$V_{\text{FCF}} = \sum_{t=1}^T \frac{\text{FCF}_T}{(1+\text{WACC})^t} + \frac{\text{TV}_{\text{FCF}}}{(1+\text{WACC})^t} + \text{ECMS} - D - PS$$

with  $\text{FCF} = (\text{Sales} - \text{OpExp} - \text{DepExp}) (1 - \tau) + (\text{DepExp} - \Delta \text{WC} - \text{CapExp})$

$V$  = Market Value

$\text{WACC}$  = Weighted Average Cost of Capital

$\text{FCF}$  = Free Cash Flow

$\text{TV}$  = Terminal Value

$\text{ECMS}$  = Excessive Cash and Marketable Securities

$D$  = Debt

$\text{OpExp}$  = Operating Expenses

$\text{DepExp}$  = Depreciation Expenses

$\text{WC}$  = Working Capital

$\text{CapExp}$  = Capital Expenditures

$PS$  = Preferred Shares

$g$  = expected FCF growth

# Estimating the Intrinsic Value

Most investment valuation involves:

Estimating the **amount** and **timing** of the cash flows

Interest, dividends, and capital gains

Estimating the **growth rate** of returns

common stock / Real estate  
(Can grow over time)

Preferred Stock / Bonds  
(fixed)

Applying an appropriate discount rate to the cash flows to estimate the investment's intrinsic value

The required return for the **risk** assumed **Amount & timing of cash flow**

Comparing the intrinsic value to the **market price**

If estimated intrinsic value > market price, then **BUY!**

## Preferred Stock

# Common Stock

## Constant (Gordon) Growth DDM • $g \leq g_{\text{economy}}$

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# The Weighted Average Cost of Capital

- The weighted average cost of capital (WACC or  $k_0$ ) is the benchmark required rate of return used by a firm to evaluate its investment opportunities
  - The discount rate used to evaluate projects of **similar risk to the firm**
- It takes into account **how** a firm finances its investments
  - How much debt versus equity does the firm employ?
- The WACC depends on...
  - Qualitative factors
  - The market values of the alternative sources of funds
  - The market costs associated with these sources of funds

# Estimating the WACC

- The main steps involved in the estimation of the WACC are...
  - Identify the financing components
  - Estimate the current (or market) values of the financing components
  - Estimate the cost of each financing component
  - Estimate the WACC
- We will consider each step for typical financing components

# Identify the Financing Components

- Debt

- Identify all externally supplied debt items
- Do not include creditors and accruals as these costs are already included in net cash flows

- Ordinary shares

- Obtain number of issued shares from the balance sheet
- Do not include reserves and retained earnings

- Preference shares

- Obtain number of issued shares from the balance sheet

# Valuing the Financing Components

- Use market values and **not** book values
- Value coupon paying debt using the following pricing relation (see Lecture 3)

$$P_0 = \frac{C_1}{(1+k_d)} + \frac{C_2}{(1+k_d)^2} + \dots + \frac{C_n}{(1+k_d)^n} + \frac{F_n}{(1+k_d)^n}$$

$$P_0 = \sum_{t=1}^n \frac{C_t}{(1+k_d)^t} + \frac{F_n}{(1+k_d)^n}$$

where       $P_0$  = Market price of the debt security  
               $C_t$  = Periodic interest payment on debt in period  $t$   
               $k_d$  = Required rate of return on debt

# Valuing Long Term Debt

**Example:** BLD Ltd has 10,000 bonds outstanding and each bond has a face value of \$1,000 with two years remaining to maturity. The bonds pay coupons (or interest) at a rate of 10% p.a. every six months. If the market interest rate appropriate for the bond is 15% p.a., what is the current price of each bond? What is the total market value of debt in BLD Ltd's capital structure?

## Valuing Long Term Debt

- Coupon (or interest) payments are made every six months
- Number of payments,  $n = 4$ , semi-annual payments
- Annual interest payments =  $0.10(1000) = \$100.00$ 
  - So, semi-annual interest payments =  $\$50.00$
- Repayment of principal at the end of year 2 =  $\$1000.00$
- Required return on debt,  $k_d = 15\%$  p.a.
- So, semi-annual required return on debt,  $k_d = 7.5\%$

# Valuing Long Term Debt

The price of the bond is...

$$P_0 = \frac{50}{(1.075)^1} + \frac{50}{(1.075)^2} + \frac{50}{(1.075)^3} + \frac{1050}{(1.075)^4}$$

$$P_0 = \$916.27$$

- So, total value of debt =  $10000(916.27) = \$9,162,700$
- **Note:** As the coupon rate is lower than the market rate, the price is less than the face value, that is, the bond is selling at a **discount** to face value
  - If the coupon rate is greater than the market rate, the price would be at a **premium** to face value

# Valuing Ordinary Shares

- **Example:** ABC Ltd has 300,000 shares on issue which each have a par value of \$1.00. If the shares are currently trading at \$3.50 each what is the total market value of ABC's ordinary shares?
- There are 300,000 shares on issue with a market value of \$3.50 per share
- Market value of equity =  $300000 \times 3.50 = \$1,050,000$ 
  - The par (or book) value of shares is **not** relevant here

# Valuing Preference Shares

- Preference shares pay a fixed dividend at regular intervals
- If the shares are non-redeemable, then the cash flows represent a perpetuity and the market value can be computed as...
- $P_0 = D_p / k_p$

Where

$P_0$  = The current market price

$D_p$  = Value of the periodic dividend

$k_p$  = Required return on preference shares

# Valuing Preference Shares

- Example: Assume the preference shares of XYZ Ltd pay a dividend of \$0.40 p.a. and the cost of preference shares is 10% p.a. What is the price of the preference shares? If XYZ Ltd has 500,000 preference shares outstanding, what is the market value of these shares?
- The cash flows from the preference shares are...
  - $D_p = \$0.40$  per share
  - So,  $P_0 = 0.40/0.10 = \$4.00$
  - Market value of shares =  $500000 \times 4.00 = \$2,000,000$

# Estimating the Costs of Capital

- The costs of a firm's financing instruments can be obtained as follows...
  - Use observable market rates - may need to be estimated
  - Use effective annual rates
  - For the cost of debt use the market yield
- Focus here is on the costs of debt, ordinary shares and preference shares
  - **Note:** We ignore the complications of flotation costs and franking credits associated with dividends (sections 15.5.3 and 15.5.5 of the text)

## Cost of Debt

- **Example:** The bonds of ABD Ltd have a face value of \$1,000 with one year remaining to maturity. The bonds pay coupons at the rate of 10 percent p.a. If the current market price of the bonds is \$1,018.50, what is the firm's cost of debt?
  - The annual interest (coupon) paid on the debt is...
    - $1000 \times 0.10 = \$100$
  - So,  $1018.50 = (1000 + 100)/(1 + k_d)$
  - $k_d = (1100/1018.50) - 1 = 8.0\%$

# Cost of Ordinary Shares

It is common to use CAPM to estimate the cost of equity capital, where the cost of equity is...

$$k_e = r_f + [E(r_m) - r_f]\beta_e$$

where  $E(r_m) - r_f$  = Expected market risk premium

$r_f$  = Risk free rate

$\beta_e$  = Equity beta

- Note that the equity beta is the estimate of the firm's relative “risk” compared to movements in the market portfolio
  - The market risk premium is typically estimated using historical market data
  - The riskfree rate is typically based on the long term government bond rate

# Cost of Ordinary Shares

**Example:** Assume that the risk free rate is 6 percent, the expected market risk premium is 8 percent and the equity beta of XYZ Ltd's equity is 1.2. What is the firm's cost of equity capital?

Using the CAPM, we have...

$$\begin{aligned} \diamond k_e &= r_f + [E(r_m) - r_f]\beta_e \\ \diamond k_e &= 0.06 + 0.08 \times 1.2 = 15.6\% \end{aligned}$$

**Note:** Can also use the dividend discount models covered in Lecture 4 (but not commonly used by managers...)

$$\begin{aligned} \diamond P_0 &= D_1 / (k_e - g) \\ \diamond \text{So, } k_e &= D_1 / P_0 + g \end{aligned}$$

# Cost of Preference Shares

- Recall that,  $P_0 = D_p/k_p$
- Thus,  $k_p = D_p/P_0$
- **Example:** The preference shares of DBB Ltd pay a dividend of \$0.50 p.a. If the preference shares are currently selling for \$4.00 per share, what is the cost of these shares to the firm?
- The cost of preference shares is given as...
$$k_p = D_p/P_0$$
$$\text{So, } k_p = 0.50/4.00 = 12.5\%$$

# Weighted Average Cost of Capital

The weighted average cost of capital ( $k_o$ ) uses the cost of each component of the firm's capital structure and weights these according to their relative market values

Assuming that only debt and equity are used, we have...

$$k_o = k_d(D/V) + k_e(E/V)$$

where  $k_d$  = Cost of debt

$k_e$  = Cost of equity

$D$  = Market value of debt

$E$  = Market value of equity

$V = D + E$

# Weighted Average Cost of Capital

Assuming that preference shares are used as well as debt and equity...

$$k_o = k_d(D/V) + k_e(E/V) + k_p(P/V)$$

where  $P$  = Market value of preference shares

$k_p$  = Cost of preference shares

$$V = D + E + P$$

- Be careful of rounding errors in initial calculations
- Be careful to work in consistent terms
  - Calculations in percentages versus decimals
- Check your answers with some common sense logic...

$$\diamond k_e > k_p > k_d > k_d(1 - t_c) \text{ (Why?)}$$

# Taxes and the WACC

- Under the classical tax system...
  - Interest on debt is tax deductible
  - Dividends have no tax effect for the firm
- The after-tax cost of debt,  $k'_d = (1 - t_c) k_d$   
where  $t_c$  corporate tax rate
- The cost of equity ( $k_e$ ) is unaffected
- The after-tax WACC is defined as...

$$k_o = k_d(1 - t_c)(D/V) + k_e(E/V) \quad \text{and}$$
$$k_o = k_d(1 - t_c)(D/V) + k_e(E/V) + k_p(P/V)$$

# Calculating and Using the WACC

**Example:** You are given the following information for BCA Ltd. Note that book values are obtained from the firm's balance sheet while market values are based on market data.

The firm's marginal tax rate is 30%. Estimate the firm's before-tax and after-tax weighted average costs of capital

	Book values	Market values	Market costs
Bonds	\$30,000,000	\$50,000,000	8.0%
Preference shares	\$10,000,000	\$20,000,000	10.0%
Ordinary shares	\$60,000,000	\$80,000,000	14.0%
Total	\$100,000,000	\$150,000,000	

# Calculating and Using the WACC

- Before-tax weighted average cost of capital
  - WACC weights are based on market values so book values are not relevant

$$k_o = k_d(D/V) + k_e(E/V) + k_p(P/V)$$
$$V = D + E + P$$

	Market values	Weights	Market costs	Weights×Costs
Bonds	\$50,000,000	0.333	8.0%	2.67%
Preference shares	\$20,000,000	0.133	10.0%	1.33%
Ordinary shares	\$80,000,000	0.533	14.0%	7.47%
Total	\$150,000,000	1.000		11.47%

**Note:** Weight in bonds,  $D/V = 50/150 = 0.333$ , and so on

- Before-tax cost of capital = **11.47%**

# Calculating and Using the WACC

The after-tax cost of capital requires the after tax **cost of debt**

$$k'_d = k_d (1 - t_c)$$

$$k'_d = 0.08(1 - 0.30) = 5.6\%$$

	Market values	Weights	After tax market costs	Weights×Costs
Bonds	\$50,000,000	0.333	5.6%	1.87%
Preference shares	\$20,000,000	0.133	10.0%	1.33%
Ordinary shares	\$80,000,000	0.533	14.0%	7.47%
Total	\$150,000,000	1.000		10.67%

- **Note:** Weight in bonds,  $D/V = 50/150 = 0.333$ , and so on
  - After-tax cost of capital = 10.67%